1. Using the relation

$$F(z) = \frac{1}{2\pi} \int_{-\infty}^{\infty} e^{ikz} \tilde{F}(k) dk ,$$

we obtain

$$\sum_{l=-\infty}^{\infty} F(lC) = \frac{1}{2\pi} \sum_{l=-\infty}^{\infty} \int_{-\infty}^{\infty} e^{iklC} \tilde{F}(k) dk$$

$$= \frac{1}{2\pi} \int_{-\infty}^{\infty} dk \tilde{F}(k) \sum_{l=-\infty}^{\infty} e^{i2\pi l \frac{kC}{2\pi}}$$

$$= \frac{1}{2\pi} \int_{-\infty}^{\infty} dk \tilde{F}(k) \sum_{p=-\infty}^{\infty} \delta\left(\frac{kC}{2\pi} - p\right)$$

$$= \frac{1}{2\pi} \sum_{p=-\infty}^{\infty} \int_{-\infty}^{\infty} \frac{2\pi \delta\left(k - \frac{2\pi p}{C}\right)}{C} \tilde{F}(k) dk$$

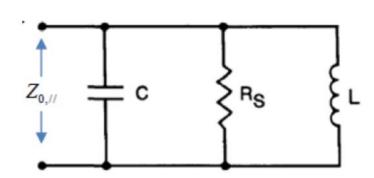
$$= \frac{1}{C} \sum_{p=-\infty}^{\infty} \tilde{F}\left(\frac{2\pi p}{C}\right)$$

where we also used

$$\delta(g(x)) = \sum_{i} \frac{\delta(x - x_{i})}{|g'(x_{i})|}$$

with x_i being the roots of g(x).

2.



The impedance is determined by

$$\begin{split} \frac{1}{Z_{0,//}} &= \frac{1}{Z_R} + \frac{1}{Z_L} + \frac{1}{Z_C} \\ &= \frac{1}{R_s} + \frac{1}{j\omega L} + j\omega C \\ &= \frac{1 + jR_s \sqrt{\frac{C}{L}} \left(\omega\sqrt{LC} - \frac{1}{\omega\sqrt{LC}}\right)}{R_s} , \\ &= \frac{1 + jQ\left(\frac{\omega}{\omega_R} - \frac{\omega_R}{\omega}\right)}{R_s} \\ &= \frac{1 + iQ\left(\frac{\omega_R}{\omega} - \frac{\omega}{\omega_R}\right)}{R_s} \end{split}$$

i.e.

$$Z_{0,//} = \frac{R_s}{1 + iQ\left(\frac{\omega_R}{\omega} - \frac{\omega}{\omega_R}\right)}$$

where
$$j = -i$$
, $Q \equiv R_s \sqrt{\frac{C}{L}}$ and $\omega_R \equiv \frac{1}{\sqrt{LC}}$.