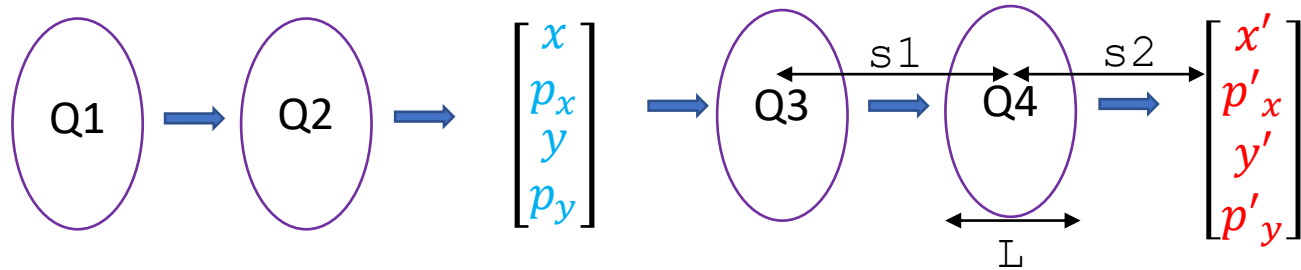


Slice Emittance Measurement

KS

29/7/2022



$$\therefore \begin{bmatrix} m_{11} & m_{12} \\ m_{21} & m_{22} \end{bmatrix} \begin{bmatrix} \omega_{11} & \omega_{12} \\ \omega_{21} & \omega_{22} \end{bmatrix} \begin{bmatrix} x \\ p_x \\ y \\ p_y \end{bmatrix} = \begin{bmatrix} x' \\ p'_x \\ y' \\ p'_y \end{bmatrix}$$

Machine Parameters

Vertical

$$\sqrt{\sigma'_y} = \frac{y'_{rms}}{\omega_{12}} \quad \xi = \frac{\omega_{11}}{\omega_{12}}$$

$$\sigma'_y = a_y \xi^2 + b_y \xi + c_y$$

Horizontal

$$\sqrt{\sigma'_x} = \frac{x'_{rms}}{m_{12}} \quad v = \frac{m_{11}}{m_{21}}$$

$$\sigma'_x = a_x v^2 + b_x v + c_x$$

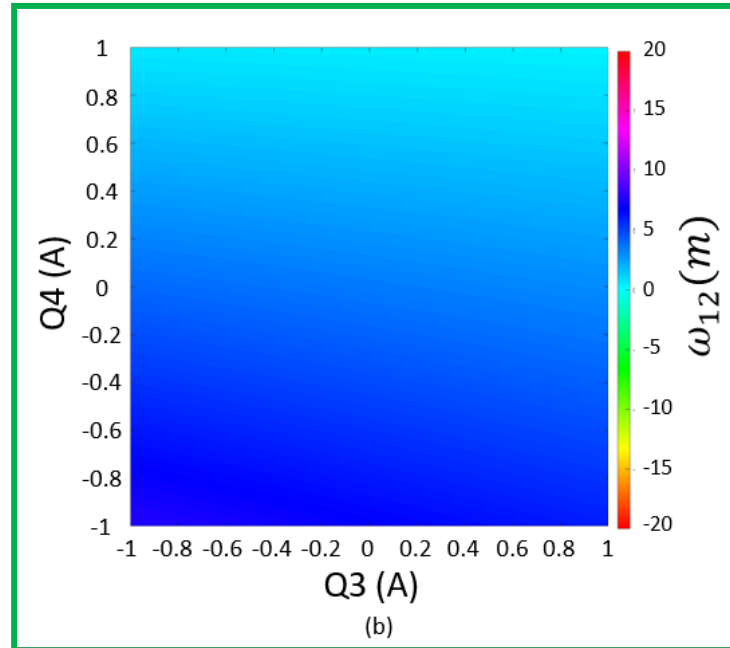
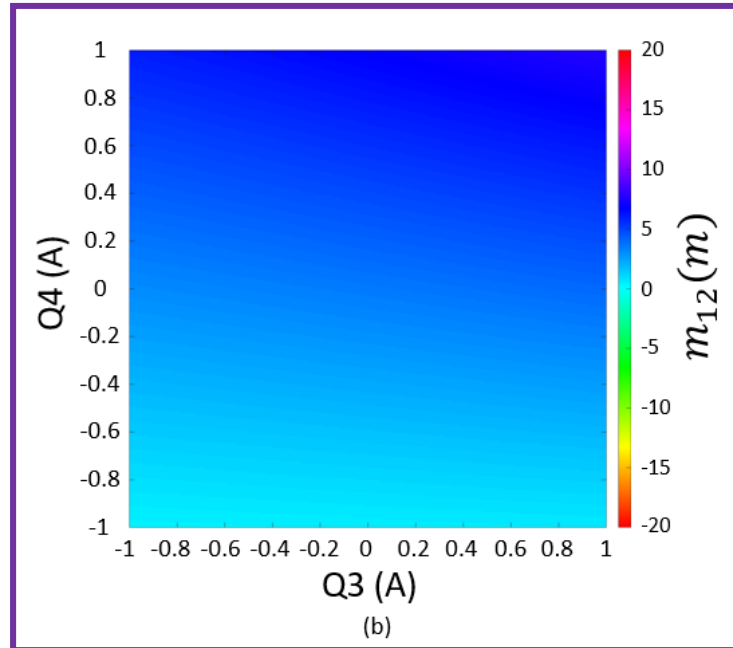
Beam Parameters

Vertical & Horizontal
Machine Parameters are related

$$\omega_{12}(Q3, Q4) = m_{12}(-Q3, -Q4)$$

$$\xi(Q3, Q4) = v(-Q3, -Q4)$$

180 deg rotation



$$\sigma'_y = a_y \xi^2 + b_y \xi + c_y$$

ξ is constant



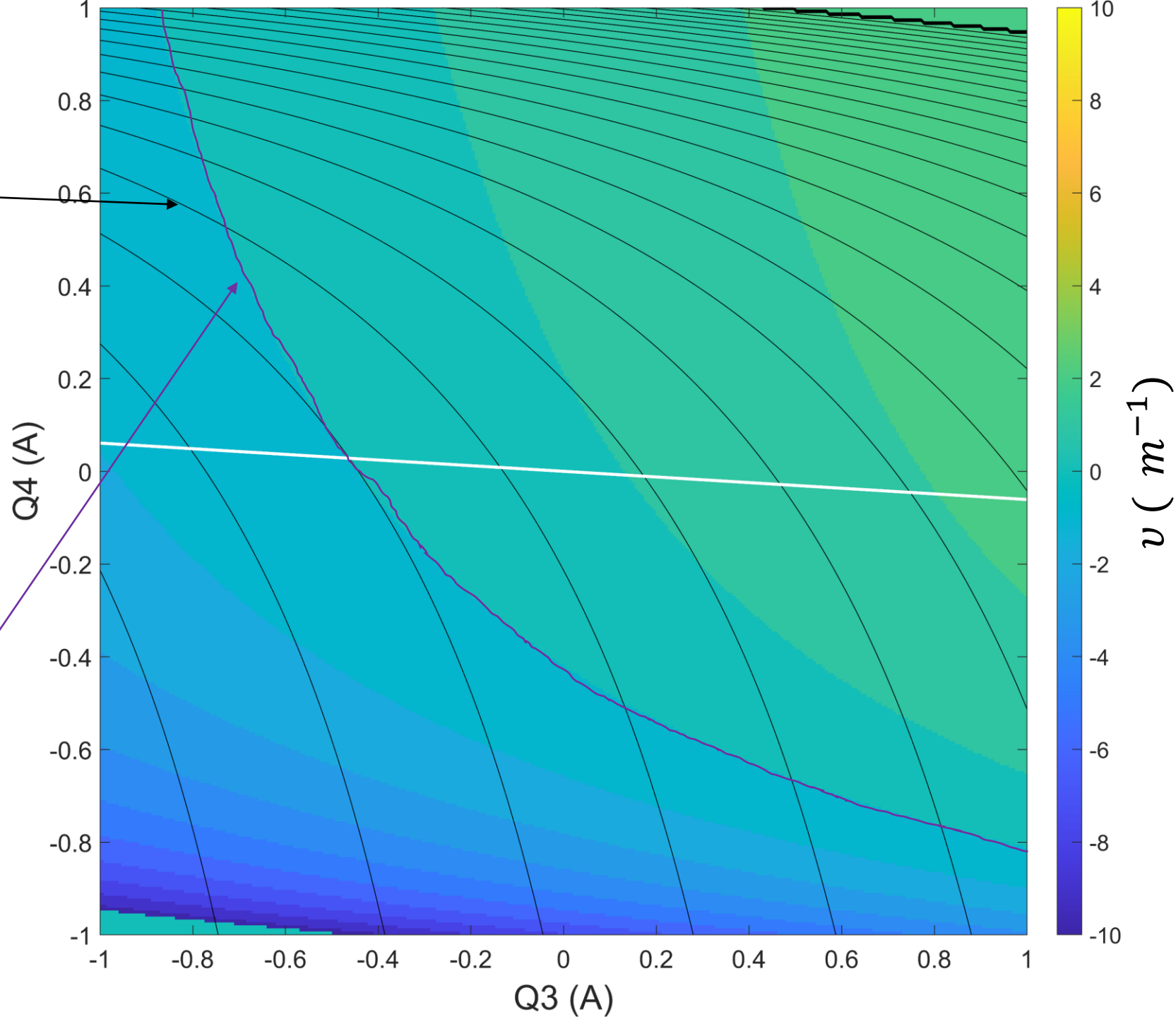
σ'_y is constant

$$\sigma'_x = a_x v^2 + b_x v + c_x$$

v is constant



σ'_x is constant



ξ is constant



σ'_y is constant $\Rightarrow \omega_{12}(Q3, Q4) \Big|_{\xi=const.} = \omega_{12}(Q4)$



Only a machine property

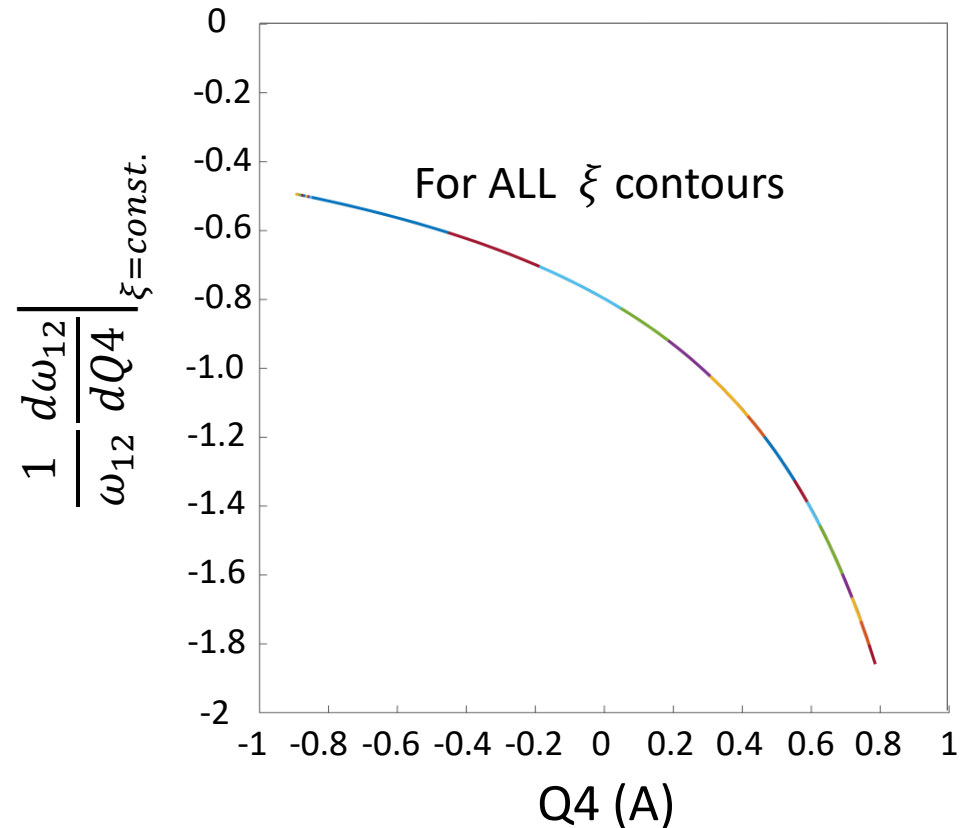
$$\left. \frac{d \ln(y'_{rms})}{dQ4} \right|_{\xi=const.} = \left. \frac{1}{\omega_{12}} \frac{d\omega_{12}}{dQ4} \right|_{\xi=const.}$$

$$\left. \frac{1}{\omega_{12}} \frac{d\omega_{12}}{dQ4} \right|_{\xi=const.} \approx \frac{1}{aQ_4 + b} + c$$

Second order term of ω_{12} $O(Q_4^2)$

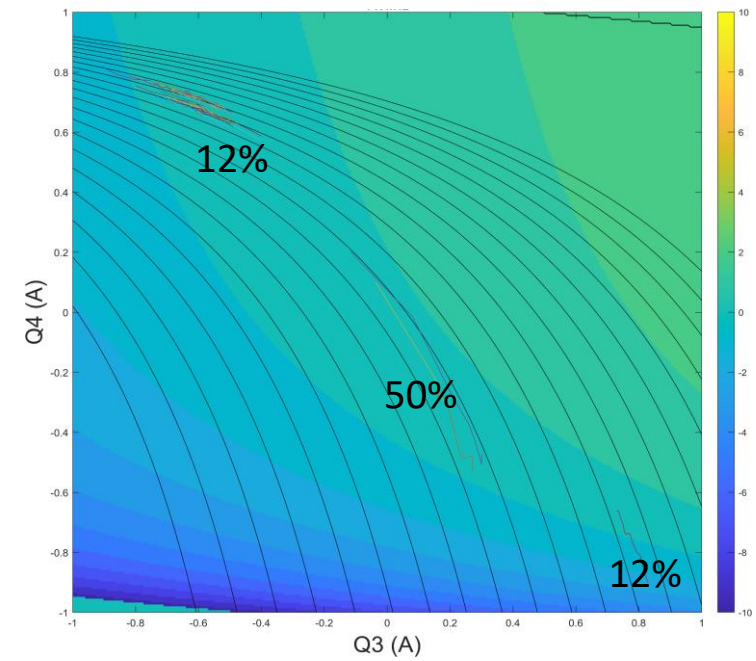
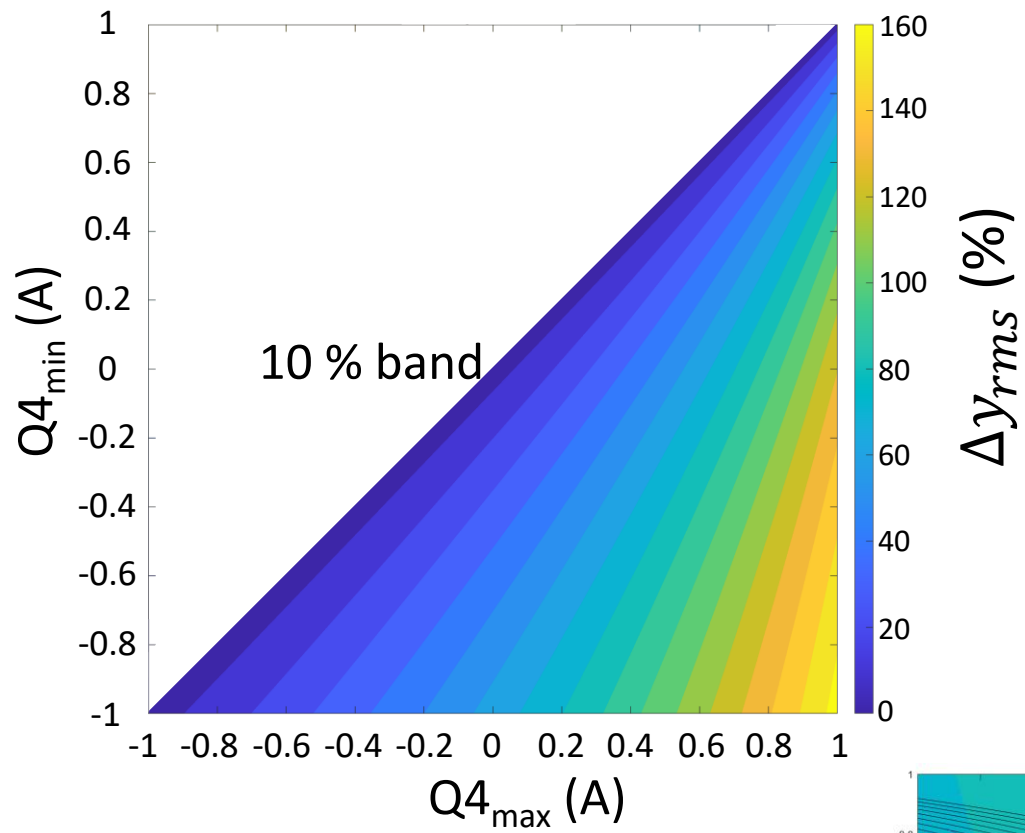
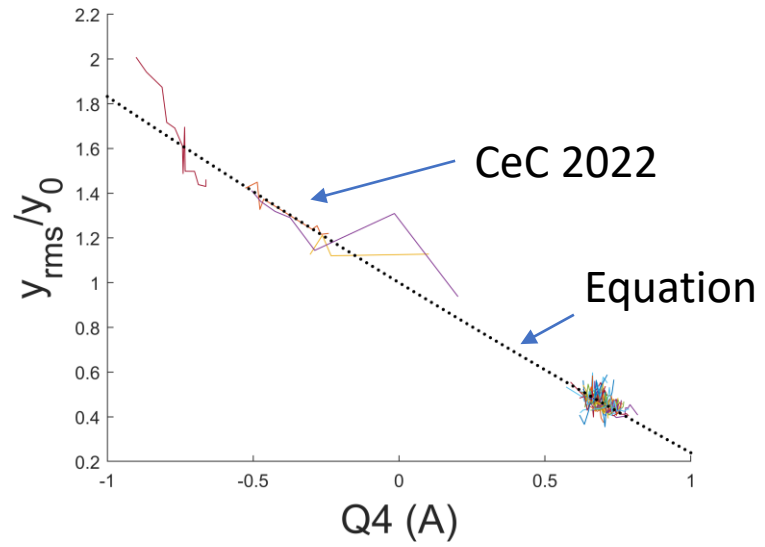
From thin lens

$$y_{rms} \Big|_{\xi=const.} = y_0 \left(\frac{a}{b} Q_4 + 1 \right)^{\frac{1}{a}} e^{c \cdot Q_4}$$



Thin lens	Thick lens
$a = 1;$	$a = 0.984620283;$
$b = -1.2534;$	$b = -1.320971736;$
$c = 0;$	$c = -0.04;$
* $b = (s1+s2) / (s1s2L*Qk)$	

$$y_{rms} \Big|_{\xi=const.} = y_0 \left(\frac{a}{b} Q_4 + 1 \right)^{\frac{1}{a}} e^{c \cdot Q_4}$$



So Q_4 range will defines time resolve resolution

- focuses beam vertically with Q3 Q4
- Test 3 points σ'_x along the ξ contour
- Set Q3 Q4 according to the changes of ν that requires
- Change Q1 Q2 to re-focuses beam vertically
- Essentially, we shifted ξ contour to where contains the minimum σ'_x

