

Home Work PHY 554 #7.

HW 1 (5 points): RF cavity beam loading/unloading.

A short ultra-relativistic ($1-v/c \ll 1$) bunch with charge of 5 nC is passing through a 0.3 meter long 500 MHz pillbox accelerating cavity operating at the fundamental TM_{010} with peak accelerating field of 5 MV/m.

(1) Find the change of the cavity voltage $\Delta V/V$ (accelerating field) after the beam passes through it as function of the phase of the beam passing the cavity. What are the maximum and minimum $\Delta V/V$?

(2) How the beam loading $\Delta V/V$ depends on the accelerating field? At what level of accelerating it reaches $\Delta V/V$ 1%?

- (a) Assume that beam does not change velocity in the cavity;
- (b) Hint – use energy conservation law
- (c) Assume that relative change of the voltage $\Delta V/V$ is small, e.g. the beam loading can be treated as a perturbation.

HW 2 (3 points): Cavities filled with ferrite material are used for RF system requiring large frequency tuning range. The frequency is controlled by applying external magnetic field, B_{ext} , to the ferrite material and by doing so to change its magnetic permeability $\mu(B_{\text{ext}})$. A 300 m in circumference AGS synchrotron accelerates polarized protons from total energy of 2.5 GeV to 25 GeV.

- (a) Calculate the range of the beam revolution frequency in AGS;
- (b) Assuming 100% filling by ferrite, what should be ratio of μ_{max} to μ_{min} . Where μ should have maximum value?

Note: RF systems operate on a fixed integer harmonic of the revolution frequency.

HW 3 (2 points): In RF cavity operating at 500 MHz, amplitude of the magnetic field at the part surface is 500 Gs or 500 Oe. Find power losses per square meter of the surface for:

- (a) Cu cavity*
- (b) SRF cavity with surface resistance, $R_s = 5 \cdot 10^{-9}$ Ohm.

How much water you can heat from 20 C° to 40 C° in one hour (3,600 second) by cooling 1m² surface in such Cu cavity?

***Hint:** you may use the conductivity of Cu or scale R_s from results shown in lectures. Thermal capacitance of water is 4,179 J/kg/ C°.