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1 (10 point): localized orbit correction

The closed orbit can be locally corrected by using steering dipoles. A commonly used algorithm is based on the "three-bumps" method, where three steering dipoles are used to adjust local-orbit distortion.

Let θ_1 , θ_2 and θ_3 be the three bump angles. For the orbit distortion to be localized between first and third dipoles, show that these angles must be related by

$$heta_2=- heta_1\sqrt{rac{eta_1}{eta_2}}\,rac{\sin\psi_{31}}{\sin\psi_{32}}, \qquad heta_3= heta_1\sqrt{rac{eta_1}{eta_3}}\,rac{\sin\psi_{21}}{\sin\psi_{32}},$$

where β_1 , β_2 and β_3 are the beta functions at local bumps and ψ_{ij} is the phase advance between ith and jth steering dipoles.

Show under what condition, the "three-bumps" method can become "two-bumps" method, i.e., only two steering dipoles are used for local orbit distortion.